

## Kinetic Analysis of the Oxidative Coupling of Methane over Na<sup>+</sup>-Doped MgO

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The reaction rate of oxidative coupling of methane was studied kinetically using 0.0165 or 0.05 g of 15% Na<sup>+</sup>-MgO catalyst at 923, 973, and 1023 K in a flow reactor under a CH<sub>4</sub> pressure of 1.36 to 13 kPa and an O<sub>2</sub> pressure of 0.36 to 4.7 kPa. The reaction rate was well expressed by the following mechanism. The kinetic data were analyzed by the Rideal-redox-type rate equation assuming methyl radical and active surface oxygen as the steady-state intermediates: (1) O<sub>2</sub> + site  $\xrightarrow{2k_1}$  active oxygen, (2) CH<sub>4</sub> + active oxygen  $\xrightarrow{k_2}$  ·CH<sub>3</sub> + OH(a) + site, (3) ·CH<sub>3</sub> + xO  $\xrightarrow{k_3}$  CO, CO<sub>2</sub>, (4) 2 ·CH<sub>3</sub>  $\xrightarrow{k_4}$  C<sub>2</sub>H<sub>6</sub>. The constants  $k_1$ ,  $k_2$ ,  $x$ , and  $k_4/k_3^2$  were obtained for every temperature. The activity is related to  $k_1$  and  $k_2$ , while the selectivity (C<sub>2</sub>/C<sub>1</sub>) is related to  $k_4/k_3^2$ . The activation energies are 18 and 36 kcal/mol for  $k_1$  and  $k_2$ , respectively. By considering the negative activation energy of  $k_3$  (-7 kcal/mol), step 3 is inferred to contain the equilibrium reaction in which ·CH<sub>3</sub> and O<sub>2</sub> form methyl peroxide if the value of  $x$  is 2.0. The actual smaller value of  $x$  suggests that part of the methyl radical is oxidized by the surface oxygen. The specific surface area effect is also explained by this reaction mechanism if we assume that  $k_3$  occurs on the surface (methyl peroxide decomposition) and  $k_4$  occurs in the gas phase. The Langmuir-Hinshelwood mechanism can also be applied; however, it leaves several ambiguous points. These conclusions are only valid at high temperatures (923 to 1023 K) and under the low conversion (both  $X_{\text{CH}_4}$  and  $X_{\text{O}_2}$  are lower than 10%), whereas the consecutive oxidation of C<sub>2</sub> compounds should be taken into account under the high conversion condition.

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### INTRODUCTION

It has proved difficult to elucidate the complete mechanism of the oxidative coupling of methane (2CH<sub>4</sub> + 0.5 O<sub>2</sub> → C<sub>2</sub>H<sub>6</sub> + H<sub>2</sub>O, 2CH<sub>4</sub> + O<sub>2</sub> → C<sub>2</sub>H<sub>4</sub> + 2H<sub>2</sub>O) over catalysts because the reaction may involve gas phase radical chain mechanisms at high temperatures (a heterogeneous-homogeneous mechanism). However, it is very important to obtain the rate equations of this reaction for catalyst and reactor design. The rate equation should hopefully be related to the reaction mechanism, so that the rate constants are related to the catalytic properties and the transport phenomena.

The kinetic results obtained so far fall into two categories. The first is the

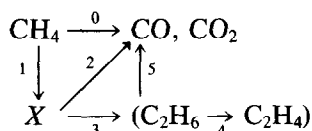
Langmuir-Hinshelwood type involving the reaction of adsorbed methane and adsorbed oxygen; an example is the reaction over Sm<sub>2</sub>O<sub>3</sub> (1). The second category is the redox type, involving the reduction of catalyst by CH<sub>4</sub> and the oxidation of it by O<sub>2</sub>; an example is the reaction over BaO and PbO-Al<sub>2</sub>O<sub>3</sub> (2, 3). The rate equations given in those reports treat only the rate of methane conversion and cannot explain the C<sub>2</sub> compound selectivity.

There are several reports in which each of the C<sub>2</sub> and C<sub>1</sub> compound formations is analyzed kinetically. Quite recently, Labinger and Ott (4) proposed a heterogeneous-homogeneous reaction mechanism in which the methyl radical is produced on the metal oxide surface, and the hydrocarbon is produced in the gas phase. They simulated their data, which was obtained by a

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pulse method over Mn-MgO, by using their steady-state model. In this study we reach the same conclusion by a simple method using Na<sup>+</sup>-MgO catalyst under steady-state conditions at various temperatures. Ali Emesh and Amenomiya derived the power rate law equation using the reaction over Bi<sub>2</sub>O<sub>3</sub>-K<sub>2</sub>CO<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> (5). They calculated the reaction order of elementary steps in the reaction network (methane to CO<sub>2</sub>, methane to C<sub>2</sub> hydrocarbons, and C<sub>2</sub> hydrocarbons to CO<sub>2</sub>), where the mechanisms do not seem to agree completely with the rate equation.

For convenience, we start by proposing the following reaction scheme:



Although we did not detect *X* (the common intermediate of C<sub>2</sub>H<sub>6</sub> and C<sub>1</sub> oxides) in this experiment, we assumed it to be ·CH<sub>3</sub>, as has been observed over similar catalysts such as Li<sup>+</sup>-MgO (6).

In general, the product ratio C<sub>2</sub>/C<sub>1</sub> over effective catalysts is higher at higher temperatures when the reactions are compared under the same space velocity condition. If C<sub>1</sub> compounds (CO, CO<sub>2</sub>) were formed exclusively through C<sub>2</sub> hydrocarbons (C<sub>2</sub>H<sub>6</sub>, C<sub>2</sub>H<sub>4</sub>) (steps 1-3-5 in the above scheme), the C<sub>2</sub>/C<sub>1</sub> ratio should be low at a high temperature, where the conversion is higher than that at a low temperature. Therefore, C<sub>1</sub> oxides and C<sub>2</sub> hydrocarbons seem to be produced independently at the start of the reaction (steps 0, 1-2, and 1-3). In our previous study, we found that CO<sub>2</sub> production occurs at a lower temperature than that needed to produce C<sub>2</sub> hydrocarbons over the less effective catalysts (7). Over those catalysts (such as Mn<sup>2+</sup>, Co<sup>2+</sup>, Ag<sup>+</sup>-doped MgO), the path of C<sub>2</sub> hydrocarbon production (steps 1-3) seems to be different from the path of C<sub>1</sub> oxide production (step 0). In

the present work we refer to reaction mechanisms of that sort as the *independent reaction model*. On the other hand, over effective catalysts such as MgO catalysts doped with alkali metal oxides, C<sub>2</sub> hydrocarbons and C<sub>1</sub> oxides start to be produced at almost the same temperature (7). Thus, it seems probable that the production of C<sub>2</sub> hydrocarbons (steps 1-3) and C<sub>1</sub> oxides (steps 1-2) has a mutual intermediate (*X*). We refer to this type of reaction mechanism as a *reaction model with a common intermediate*. This mechanism is essentially the same as those proposed by Lunsford and colleagues (6, 8).

In the preceding paper, the effect of adding alkali metal to MgO was studied and was attributed to the two factors: chemical and physical (7, 9-11). Alkali increased the lattice distortion, which could cause an increase in surface active sites (chemical factor), and it also decreased the specific surface area of the catalyst (physical factor). Various materials that have been reported to be effective for this reaction (1-36) have low specific surface areas. For example, the surface areas of Li<sup>+</sup>-MgO (6, 14), PbO-Al<sub>2</sub>O<sub>3</sub> (12, 13), and Sm<sub>2</sub>O<sub>3</sub> (17) are 8.9, 15, and 2 m<sup>2</sup> g<sup>-1</sup>, respectively. Although the effects of specific surface area are not discussed, a decrease of specific surface area has been observed when alkali or PbO metal was added. These physical factors must be derived from the reaction mechanism, which is related to the specific surface area.

In this work, the kinetics of oxidative coupling of methane over 15% Na<sup>+</sup>-MgO (one of the most effective catalysts for this reaction) was studied to elucidate the mechanism and to obtain a suitable rate equation. The mechanism must explain several characteristics of the reaction, such as the high C<sub>2</sub> selectivity at high temperature and the specific surface area effect (physical factor).

To avoid the complexity of the algebraic treatment of rate equations, we often use the following approximation in this study:

$KP^i/(1 + KP^i)$  is replaced with  $KP^j$  ( $0 < j < i$ ), where  $P$  is the pressure and  $K$ ,  $i$ , and  $j$  are the constants.

## METHODS

### Procedure

The catalyst preparation, the pretreatment, the flow reaction apparatus, and the analysis of reactants and products were the same as in our preceding work (11). To take the kinetic data, 0.0165–0.05 g of 15%  $\text{Na}^+$ – $\text{MgO}$  catalyst was used. Up to 4 g of the catalyst was used to examine the catalyst weight/flow rate ( $W/F$ ) dependence of the reaction. Since active materials are sometimes adhered to the reactor wall, blank runs were carried out to check that the wall reaction was negligible.  $\text{C}_2$  hydrocarbons are defined as the sum of ethene and ethane, and  $\text{C}_1$  oxides are defined as the sum of  $\text{CO}$  and  $\text{CO}_2$ . A very small amount of hydrogen was detected but not measured quantitatively.

### $W/F$ Dependence of the Reaction

As a preliminary, experimental runs with various  $W/F$  ratios were carried out by changing the catalyst weight under a total flow rate of 55  $\text{ml}_{\text{NTP}}/\text{min}$  with 3.0 and 1.5 kPa of  $P_{\text{CH}_4}$  and  $P_{\text{O}_2}$  at 1023 K. The data obtained from the flow rate change sometimes differed from the data obtained from the weight change, probably because of the nature of the heterogeneous–homogeneous mechanism. No activity change was observed during the 3-h run for any sample. When more than 0.1 g of catalyst was used ( $W/F = 0.002 \text{ g min/ml}$ ),  $\text{C}_2$  and  $\text{C}_1$  production rates did not increase linearly, probably because of the remarkable  $\text{O}_2$  pressure drop at the outlet of the reactor. However, it is interesting to note that the  $\text{C}_2/\text{C}_1$  ratio is almost constant up to 0.3 g of catalyst ( $W/F = 0.006 \text{ g min/ml}$ ). This means that the production of  $\text{C}_2$  hydrocarbons (steps 1–3) and  $\text{C}_1$  oxides (steps 1–2) occur in a parallel way, and that formation of  $\text{C}_1$  oxides from  $\text{C}_2$  hydrocarbons (steps 5) would

be neglected at the beginning of the reaction. The consecutive reaction path from  $\text{C}_2$  hydrocarbons to  $\text{C}_1$  oxides (step 5) seems to be important when catalyst weight is more than 0.5 g ( $W/F = 0.01 \text{ g min/ml}$ ). The  $\text{O}_2$  conversion becomes almost 100% above 1 g of catalyst weight ( $W/F = 0.08 \text{ g min/ml}$ ). The ethene/ethane ratio increases from 0.1 g of catalyst ( $W/F = 0.002 \text{ g min/ml}$ ) to 4 g of catalyst ( $W/F = 0.08 \text{ g min/ml}$ ). Therefore,  $\text{C}_2\text{H}_4$  seems to be a secondary product via  $\text{C}_2\text{H}_6$  from  $\text{CH}_4$ . For comparison, oxidation of pure  $\text{C}_2\text{H}_6$  was carried out both with 0.018 g of 15%  $\text{Na}^+$ – $\text{MgO}$  and without catalyst at 1023 K. Table 1 shows the results.  $\text{C}_2\text{H}_4$  was the main product in both runs. Note that the reaction does occur without the catalyst. The partial pressure of  $\text{C}_2\text{H}_6$  at the blank run (no catalyst) was about 20 times higher than the partial pressure of  $\text{C}_2\text{H}_6$  produced in the run with oxidative coupling. However, the ethane-to-ethene path (step 4) seems to proceed in the gas phase in the oxidative-coupling system at 1023 K.

### Rate Measurement at Low Conversion under Various Temperatures and Pressures

The activity was measured by changing temperature,  $P_{\text{CH}_4}$ , and  $P_{\text{O}_2}$ .  $P_{\text{CH}_4}$  and  $P_{\text{O}_2}$  were controlled by changing the flow rate of

TABLE I  
Ethane Oxidation with and without Catalyst<sup>a</sup>

Product	Yield (%)	
	Blank (without catalyst)	15% $\text{Na}^+$ – $\text{MgO}^b$
$\text{CH}_4$	8.2	7.6
$\text{C}_2\text{H}_4$	54.3	54.1
$\text{CO}$	21.8	17.5
$\text{CO}_2$	0.7	2.9

<sup>a</sup> Reaction temperature was 1023 K; feed rates were as follows:  $\text{C}_2\text{H}_6 = 1.5 \text{ ml/min}$ , air = 3.75 ml/min, He = 50 ml/min.

<sup>b</sup> Catalyst weight = 0.018 g.

CH<sub>4</sub>, O<sub>2</sub>, and He. The total flow rate was usually 55 ml<sub>NTP</sub>/min (135 mmol/h). At a temperature of 923 K, 16 runs were carried out over 0.05 g 15% Na<sup>+</sup>-MgO under a CH<sub>4</sub> pressure of 1.81 to 13.0 kPa and an O<sub>2</sub> pressure of 0.40 to 4.71 kPa. At 973 K, 15 runs were carried out over 0.0165 or 0.05 g of 15% Na<sup>+</sup>-MgO under a CH<sub>4</sub> pressure of 1.36 to 13.0 kPa and an O<sub>2</sub> pressure of 0.36 to 3.98 kPa. At 1023 K, 15 runs were carried out over 0.0165 g of 15% Na<sup>+</sup>-MgO under a CH<sub>4</sub> pressure of 1.36 to 13.0 kPa and an O<sub>2</sub> pressure of 0.36 to 3.98 kPa. The CH<sub>4</sub> and O<sub>2</sub> conversions were kept at less than about 10%. C<sub>2</sub> formation rates were 2.7 to 9.8 μmol/h at 923 K, 2.6 to 23.5 μmol/h at 973 K, and 12.6 to 53.2 μmol/h at 1023 K. C<sub>1</sub> formation rates were 37 to 299, 34 to 195, and 21 to 285 μmol/h, respectively. No significant deactivation was observed over several runs, and the activity did not change when the sample was replaced with another sample of the same batch.

## RESULTS

### Power Rate Law Expression

Of the 46 runs, some were carried out at constant CH<sub>4</sub> pressure or O<sub>2</sub> pressure to give the simple pressure dependence. Figure 1 shows the CH<sub>4</sub> and O<sub>2</sub> pressure de-

TABLE 2  
Apparent Reaction Orders for  $R_{\text{CH}_4}$ ,  $R_2$ , and  $R_1$  on 0.0165 or 0.05 g 15% Na<sup>+</sup>-MgO

	Order at 923 K		Order at 973 K		Order at 1023 K	
	CH <sub>4</sub>	O <sub>2</sub>	CH <sub>4</sub>	O <sub>2</sub>	CH <sub>4</sub>	O <sub>2</sub>
$R_{\text{CH}_4}^a$	0.7	0.6	0.3	0.7	0.3	0.8
$R_2^b$	1.3	-0.4	0.5	0.1	0.5	0.2
$R_1^c$	0.7	0.7	0.3	0.9	0.3	1.0

<sup>a</sup>  $2R_2 + R_1$  (rate of methane consumption).

<sup>b</sup> Rate of C<sub>2</sub> (C<sub>2</sub>H<sub>6</sub> + C<sub>2</sub>H<sub>4</sub>) formation.

<sup>c</sup> Rate of C<sub>1</sub> (CO + CO<sub>2</sub>) formation.

pendences of the methane conversion rate over 15% Na<sup>+</sup>-MgO at 1023 K. The reaction orders of CH<sub>4</sub> and O<sub>2</sub> for the methane conversion rate at 1023 K are 0.3 and 0.8, respectively. The reaction orders at 923 and 973 K were also obtained and are given in Table 2. The rate of total CH<sub>4</sub> conversion has an order of reaction between 0 and 1 for both methane and oxygen pressures. The same tendency has been found for the results over Sm<sub>2</sub>O<sub>3</sub> (1) and BaO (3).

Figure 2 shows the formation rate of C<sub>2</sub> hydrocarbons and C<sub>1</sub> oxides over 15% Na<sup>+</sup>-MgO at 1023 K as a function of the CH<sub>4</sub> and O<sub>2</sub> pressures. The reaction orders

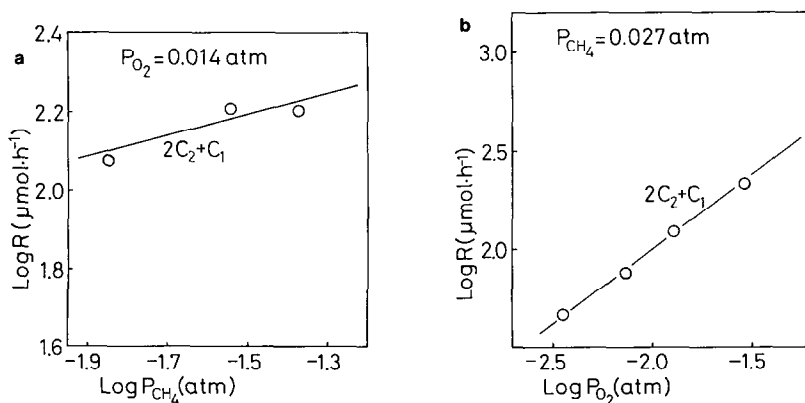


FIG. 1. CH<sub>4</sub> pressure dependence (a) and O<sub>2</sub> pressure dependence (b) for the methane conversion rate over 0.0165 g of 15% Na<sup>+</sup>-MgO at 1023 K.

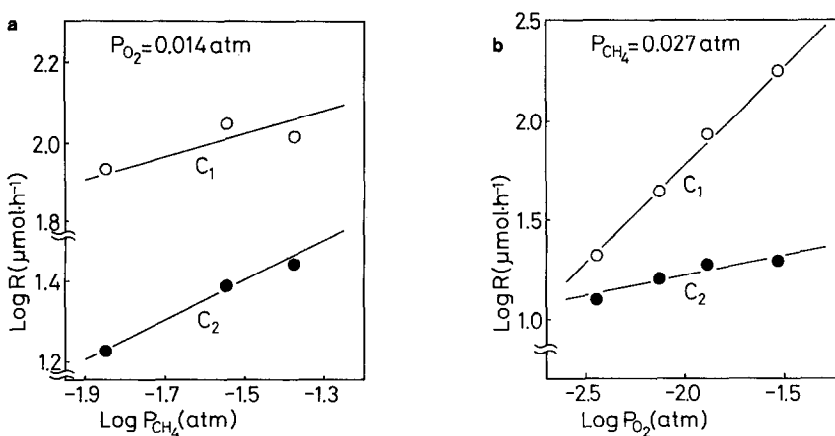


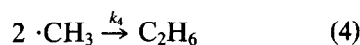
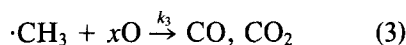
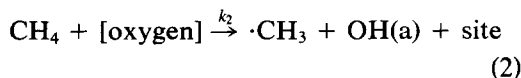
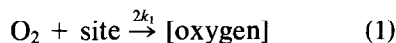
FIG. 2. CH<sub>4</sub> pressure dependence (a) and O<sub>2</sub> pressure dependence (b) for the C<sub>2</sub> and C<sub>1</sub> hydrocarbon formation rate over 0.0165 g of 15% Na<sup>+</sup>-MgO at 1023 K.

of CH<sub>4</sub> and O<sub>2</sub> for the rate of C<sub>2</sub> and C<sub>1</sub> formation at the three temperatures are given in Table 2. At all three temperatures, the CH<sub>4</sub> pressure dependence for C<sub>2</sub> formation was higher than that for C<sub>1</sub> formation; this finding is related to the fact that 1 mol of C<sub>2</sub>H<sub>6</sub> is produced from 2 mol of CH<sub>4</sub>, whereas 1 mol of CO<sub>2</sub> is produced from 1 mol of CH<sub>4</sub>. The O<sub>2</sub> pressure dependence for C<sub>2</sub> formation was lower than that for C<sub>1</sub> formation. The relation between these results and the reaction model is described in detail under Discussion.

#### Kinetic Simulation Based on the Rideal-Redox Mechanism

Several models are discussed in this work. First, we consider a mechanism referred to as the Rideal-redox mechanism, which is based on the following three assumptions. (i) The gas phase methyl radical ( $\cdot\text{CH}_3$ ), which is expected to be the intermediate of this reaction, is produced from gas phase methane and adsorbed oxygen. (ii) The surface oxygen supplied from O<sub>2</sub> and consumed by CH<sub>4</sub> is at a steady state. (iii)  $\cdot\text{CH}_3$  is converted to C<sub>2</sub>H<sub>6</sub> by coupling and to CO<sub>2</sub> by oxidation, and it is also at a steady state. In the following reaction mechanism, [oxygen] indicates an active

surface oxygen, and  $x\text{O}$  indicates the oxygen species that oxidize the methyl radical to CO<sub>2</sub>.  $x\text{O}$  is a symbol of active oxygen which cannot be determined exactly at this moment. Afterward this is assumed to be the mixture of the gas phase O<sub>2</sub> (main species) and the surface oxygen (subspecies). Symbol  $x\text{O}$  is used so that the reader may easily note the kinetic expression. Secondary reactions from ethane to ethene or from ethene to CO, CO<sub>2</sub> are neglected because of the low conversion.



Equations (1) and (2) indicate a redox of surface oxygen (redox mechanism) and Eq. (2) indicates no adsorption of methane (Rideal mechanism). For simplicity and to conform with the previous report (4), in Eq. (1) the adsorption rate of O<sub>2</sub> is assumed to be proportional to the O<sub>2</sub> pressure and the concentration of the active site. If O<sub>2</sub>

reacts with two sites, the rate should be proportional to square of the site, but at low concentrations of the adsorbed oxygen the two cases do not differ much. Therefore, we cannot decide the form of active oxygen, O(a) or O<sub>2</sub>(a), here. By using a steady-state treatment for [oxygen] in Eqs. (1) and (2), the following equations are obtained, where  $\theta$  is coverage of surface-active oxygen:

$$\frac{d\theta}{dt} = k_1 P_{O_2}(1 - \theta) - k_2 P_{CH_4}\theta = 0 \quad (5)$$

$$\theta = \frac{k_1 P_{O_2}}{k_1 P_{O_2} + k_2 P_{CH_4}} \quad (6)$$

By using a steady-state treatment of  $\cdot CH_3$  in Eqs. (2), (3), and (4), and substituting  $\theta$  in these equations with Eq. (6), Eq. (7) is obtained. In this case, the oxidation rate of  $\cdot CH_3$  is assumed to be proportional to  $P_{O_2}^{x/2}$  in Eq. (3) and the meaning of  $x$  will be discussed later:

$$\frac{dP_{\cdot CH_3}}{dt} = \frac{k_1 P_{O_2} k_2 P_{CH_4}}{k_1 P_{O_2} + k_2 P_{CH_4}} - k_3 P_{\cdot CH_3} P_{O_2}^{x/2} - 2k_4 P_{\cdot CH_3}^2 = 0 \quad (7)$$

By resolving this equation,  $P_{\cdot CH_3}$  is obtained:

$$P_{\cdot CH_3} = \frac{k_3 P_{O_2}^{x/2}}{4k_4} \left( \left( 1 + \frac{8k_1 k_2 k_4 P_{O_2} P_{CH_4}}{k_3^2 P_{O_2}^x (k_1 P_{O_2} + k_2 P_{CH_4})} \right)^{0.5} - 1 \right) \quad (8)$$

For convenience, we define

$$k_1 P_{O_2} = A \quad (9)$$

$$k_2 P_{CH_4} = B \quad (10)$$

$$\frac{k_4}{k_3^2 P_{O_2}^x} = C \quad (11)$$

Then, the following two equations are obtained:

$$\begin{aligned} \frac{dP_{C_2H_6}}{dt} &= R_2 = k_4 P_{\cdot CH_3}^2 \\ &= \frac{1}{16C} \left( \left( 1 + 8C \frac{AB}{A+B} \right)^{0.5} - 1 \right)^2 \quad (12) \end{aligned}$$

$$\begin{aligned} \frac{dP_{CO_2}}{dt} &= R_1 = k_3 P_{\cdot CH_3} P_{O_2}^{x/2} \\ &= \frac{1}{4C} \left( \left( 1 + 8C \frac{AB}{A+B} \right)^{0.5} - 1 \right). \quad (13) \end{aligned}$$

In other words, the formation rates of C<sub>2</sub> compounds and C<sub>1</sub> oxides have been obtained as a function of  $P_{CH_4}$  and  $P_{O_2}$ .

$C$  (Eq. (11)) can be obtained as  $C = R_2/R_1^2$  by Eqs. (12) and (13). We multiplied the C<sub>1</sub> and C<sub>2</sub> formation rates obtained over 0.0165 g of catalyst at 973 and 1023 K by a factor of 0.05/0.0165 in order to compare the activity with the same catalyst weight. Figure 3 shows the values of  $C$  plotted as a function of  $P_{O_2}$  at the three temperatures, where the straight lines represent Eq. (11). It can be seen that the relations between  $C$  and  $P_{O_2}$  are independent of reaction temperature; that is, the order of  $P_{O_2}$  is  $-1.6$  ( $x = 1.6$ ). The reason for this result is discussed later. By using  $C$  and  $P_{O_2}$  for each data point, we calculated  $CP_{O_2}^{1.6}$  (that is,  $k_4/k_3^2$ ). The mean value of  $k_4/k_3^2$  at each temperature is shown in Table 3. The rate of methane conversion is calculated as  $2R_2 + R_1$ , which gives  $AB/(A+B)$  (from Eqs. (12) and (13)). Figure 4 shows  $P_{O_2}(A+B)/AB = 1/k_1 + 1/k_2$  ( $P_{O_2}/P_{CH_4}$ ) plotted as a function of  $P_{O_2}/P_{CH_4}$ . The ordinate crossing gives  $1/k_1$  and the slope gives  $1/k_2$ . The values of  $k_1$  and  $k_2$  obtained at each temperature are shown in Table 3. The temperature effect of  $k_1$  and  $k_2$  gives the activation energies ( $E_1$  and  $E_2$ ) of Eqs. (1) and (2):  $E_1$  (the activation energy of the oxidation of the catalyst by O<sub>2</sub>) is  $18 \pm 3$

TABLE 3

Constants of the Reaction Rates on the Basis of the Rideal-Redox Mechanism<sup>a</sup>

	923 K	973 K	1023 K
$k_1$	0.152	0.162	0.39
$k_2$	0.079	0.23	0.53
$k_4/k_3^2$	0.76	1.77	1.57
$x$	1.60	1.60	1.60

<sup>a</sup> Values were rearranged per constant catalyst weight (0.05 g 15% Na<sup>+</sup>-MgO). The units used were kPa and mmol/h.

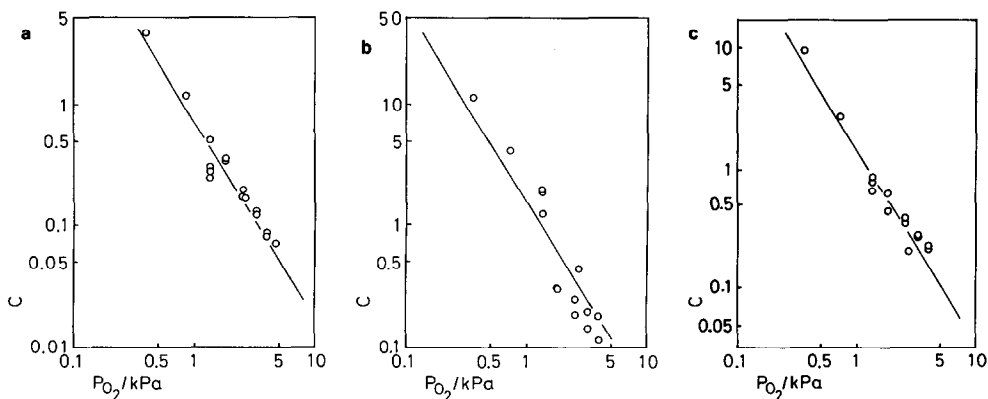
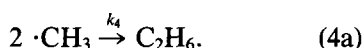
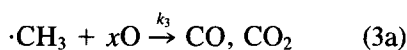
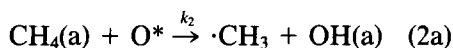
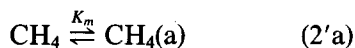


FIG. 3.  $O_2$  pressure dependence for  $C$  over 0.05 g of 15%  $Na^+$ -MgO at 923 K (a), at 973 K (b), and at 1023 K (c). See text for  $C$  ( $C = R_2/R_1^2$ ).

$kcal\ mol^{-1}$ , and  $E_2$  (the activation energy of the reduction of the catalyst by  $CH_4$ ) is  $36 \pm 3\ kcal\ mol^{-1}$ .

#### Kinetic Simulation based on the Langmuir-Hinshelwood Mechanism

In this section, we consider the so-called Langmuir-Hinshelwood mechanism, which involves the following assumptions. (i) The gas phase  $\cdot CH_3$ , an expected intermediate of this reaction, is produced by the reaction of adsorbed methane and adsorbed oxygen. (ii)  $\cdot CH_3$  is converted to  $C_2H_6$  by coupling and converted to  $CO_2$  by oxidation, and the radical is at a steady state. We do not specify the form of adsorbed methane ( $CH_4(a)$ ), of adsorbed oxygen ( $O^*$ ) that reacts with methane, or of oxygen ( $xO$ ) that reacts with  $\cdot CH_3$ . The reaction mechanism including the tentative intermediates is



Equations (1a) through (13a) in this section correspond to Eqs. (1) through (13) in the preceding section. Although  $\theta_{O^*}$  and  $\theta_{CH_4(a)}$  in Eqs. (1a) and (2'a) should be treated with the Langmuir-Hinshelwood type equation,  $KP/(1 + KP)$ , the Freundlich type, which is an approximation of the Langmuir-Hinshelwood type, is used for convenience:

$$\theta_{O^*} = K_0 P_{O_2}^b \quad (5a)$$

$$\theta_{CH_4(a)} = K_m P_{CH_4}^q \quad (6a)$$

By assuming a steady state of  $\cdot CH_3$  in Eqs. (2a), (3a), and (4a), and substituting  $\theta_{O^*}$  and  $\theta_{CH_4(a)}$  with Eqs. (5a) and (6a), Eq. (7a) is obtained. The oxidation rate of  $\cdot CH_3$  is assumed to be proportional to  $P_{O_2}^{x/2}$ :

$$\begin{aligned} \frac{dP_{\cdot CH_3}}{dt} &= k_2 \theta_{O^*} \theta_{CH_4(a)} \\ &\quad - k_3 P_{\cdot CH_3} P_{O_2}^{x/2} - 2k_4 P_{\cdot CH_3}^2 \\ &= k_2 K_0 K_m P_{O_2}^b P_{CH_4}^q - k_3 P_{\cdot CH_3} P_{O_2}^{x/2} \\ &\quad - 2k_4 P_{\cdot CH_3}^2 = 0. \end{aligned} \quad (7a)$$

By resolving this equation,  $P_{\cdot CH_3}$  is obtained:

$$P_{\cdot CH_3} = \frac{k_3 P_{O_2}^{x/2}}{4k_4} \left( \left( 1 + \frac{8k_2 k_4 K_0 K_m P_{O_2}^b P_{CH_4}^q}{k_3 P_{O_2}^x} \right)^{0.5} - 1 \right). \quad (8a)$$

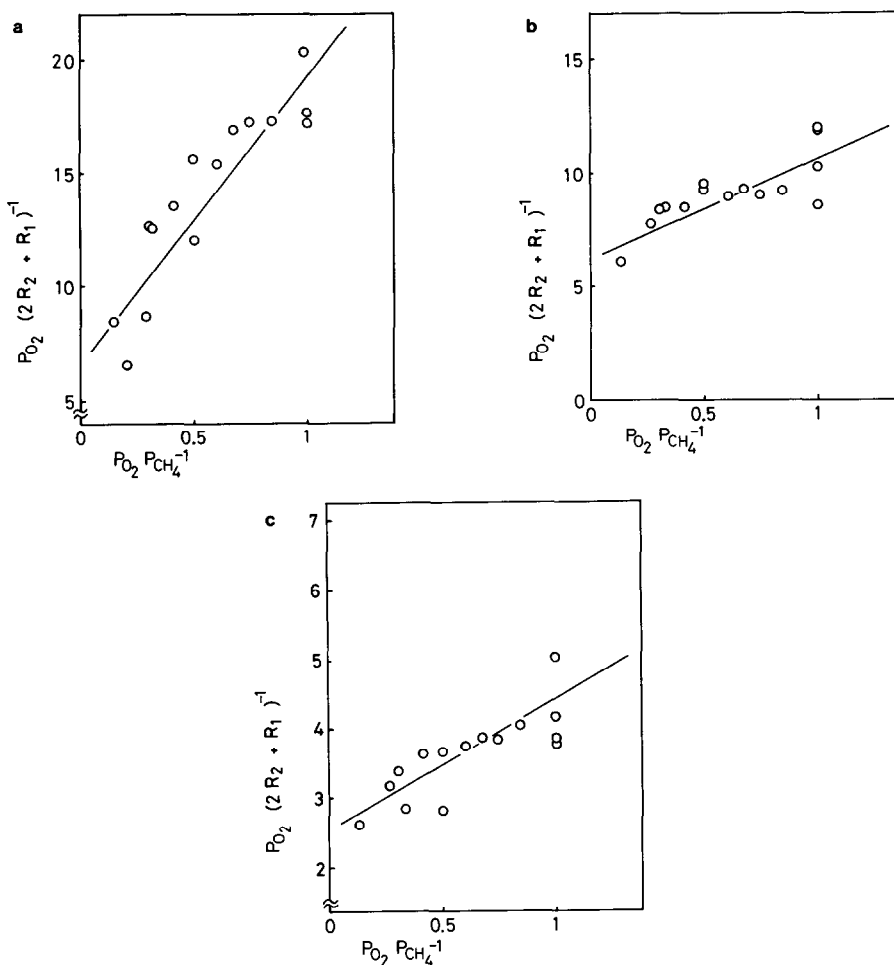


FIG. 4.  $P_{O_2}/(2R_2 + R_1)$  as a function of  $P_{O_2}/P_{CH_4}$  over 0.05 g of 15% Na<sup>+</sup>-MgO at 923 K (a), at 973 K (b), and at 1023 K (c).  $(2R_2 + R_1)$  is identical to  $R_{CH_4}$  (rate of methane conversion). See text.

For convenience, the following two equations are defined:

$$K_0 P_{O_2}^p = A' \quad (9a)$$

$$K_m P_{CH_4}^q = B' \quad (10a)$$

The formation rate of C<sub>2</sub> hydrocarbons and C<sub>1</sub> oxides is then obtained as follows, using A' and B' as well as C from Eq. (11),

$$\begin{aligned} \frac{dP_{C_2H_6}}{dt} &= R_2 = k_4 P_{CH_3}^2 \\ &= \frac{1}{16C} \left( \left( 1 + 8k_2 A' B' C \right)^{0.5} - 1 \right)^2 \quad (12a) \end{aligned}$$

$$\begin{aligned} \frac{dP_{CO_2}}{dt} &= R_1 = k_3 P_{CH_3} P_{O_2}^{x/2} \\ &= \frac{1}{4C} \left( \left( 1 + 8k_2 A' B' C \right)^{0.5} - 1 \right). \quad (13a) \end{aligned}$$

The values of C can be obtained as  $C = R_2/R_1^2$  by Eqs. (12a) and (13a); i.e., the value of C in this model is identical to that for the Rideal-redox mechanism. Therefore, the order of  $P_{O_2}$  against C is also -1.6 ( $x = 1.6$ ). Equations (12a) and (13a) give the relation  $k_2 A' B' = 2R_2 + R_1$ , which can be calculated for each data point. By taking the loga-



TABLE 4  
 Constants of Reaction Rates on the Basis of the  
 Langmuir-Hinshelwood Mechanism

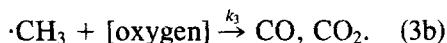
	923 K	973 K	1023 K
$p$	0.55	0.66	0.76
$q$	0.68	0.33	0.27
$k_2K_0K_m^a$	10.1	7.2	21.0
$k_4/k_3^2$	0.761	1.77	1.57
$x$	1.60	1.60	1.60

<sup>a</sup> Values were rearranged per constant catalyst weight (0.05 g of 15% Na<sup>+</sup>-MgO). The units used were kPa and mmol/h.

ritms of  $k_2A'B' = k_2K_0K_mP_{O_2}^pP_{CH_4}^q$  ( $= 2R_2 + R_1$ ) as a function of  $\log P_{O_2}$  and  $\log P_{CH_4}$  with constant  $P_{O_2}$  or  $P_{CH_4}$ ,  $p$  and  $q$  are calculated. The values of  $p$  and  $q$  are practically the same as the values of O<sub>2</sub> and CH<sub>4</sub> order in CH<sub>4</sub> conversion ( $2R_1 + R_1$ ) in Table 2. The values at each temperature are listed in Table 4. It is thus seen that the experimental data can be also rearranged by the Langmuir-Hinshelwood mechanism.

#### Kinetic Simulation Based on the Multiple-Redox Mechanism

In the Rideal-redox mechanism, the reduction of the catalyst is assumed to be performed with CH<sub>4</sub> alone. In the multiple-redox mechanism, the reductant is assumed to be both CH<sub>4</sub> and  $\cdot\text{CH}_3$ . The other assumptions are the same as for the Rideal-redox mechanism. Equations (1), (2), and (4) are also applicable to this model, and  $xO$  from Eq. (3) is assumed to be identical with [oxygen]:



Now, by using the steady-state treatment for [oxygen] in Eqs. (1), (2), and (3b), Eqs. (5b) and (6b) are obtained. In this case, the rate of Eq. (1) is assumed to be proportional to  $P_{O_2}^{0.5}$  (another case in which the rate of Eq. (1) is proportional to  $P_{O_2}$  will be described later):

$$\frac{d\theta}{dt} = k_1P_{O_2}^{0.5}(1 - \theta) - k_2P_{CH_4}\theta - k_3P_{\cdot\text{CH}_3}\theta = 0 \quad (5b)$$

$$\theta = \frac{k_1P_{O_2}^{0.5}}{k_2P_{CH_4} + k_3P_{\cdot\text{CH}_3} + k_1P_{O_2}^{0.5}} \quad (6b)$$

By using the steady-state treatment for  $\cdot\text{CH}_3$  in Eqs. (2), (3b), and (4) and substituting  $\theta$  in Eq. (5b) with Eq. (6b), the following equation is obtained:

$$\begin{aligned} \frac{dP_{\cdot\text{CH}_3}}{dt} &= k_2P_{CH_4}\theta - k_3P_{\cdot\text{CH}_3}\theta - 2k_4P_{\cdot\text{CH}_3}^2 \\ &= \frac{k_1k_2P_{O_2}^{0.5}P_{CH_4}}{k_2P_{CH_4} + k_3P_{\cdot\text{CH}_3} + k_1P_{O_2}^{0.5}} \\ &\quad - \frac{k_1k_3P_{O_2}^{0.5}P_{\cdot\text{CH}_3}}{k_2P_{CH_4} + k_3P_{\cdot\text{CH}_3} + k_1P_{O_2}^{0.5}} \\ &\quad - 2k_4P_{\cdot\text{CH}_3}^2 = 0. \quad (7b) \end{aligned}$$

Therefore,

$$2k_3k_4P_{\cdot\text{CH}_3}^3 + 2k_4(k_1P_{O_2}^{0.5} + k_2P_{CH_4})P_{\cdot\text{CH}_3}^2 + k_1k_3P_{O_2}^{0.5}P_{\cdot\text{CH}_3} - k_1k_2P_{O_2}^{0.5}P_{CH_4} = 0. \quad (8b)$$

Equation 8b cannot be solved easily because the  $P_{\cdot\text{CH}_3}$  term is third-order. Therefore, numerical calculations were performed to obtain  $P_{\cdot\text{CH}_3}$  by assuming 27 cases for which each of the constant ratios  $k_1/k_4$ ,  $k_2/k_4$ , and  $k_3/k_4$  had values of 1, 10, and 100, respectively, in order to cover the wide conditions which cannot be expected a priori. At last, several practical values of  $P_{CH_4}$  and  $P_{O_2}$  were introduced in order to obtain  $P_{\cdot\text{CH}_3}$  for the 27 cases. These hundreds values of  $P_{\cdot\text{CH}_3}$  calculated can be used to obtain the rates of formation of C<sub>2</sub> hydrocarbons (by Eq. (12b)) and of C<sub>1</sub> oxides (by Eq. (13b)):

$$\frac{dP_{C_2H_6}}{dt} = R_2 = k_4P_{\cdot\text{CH}_3}^2 \quad (12b)$$

$$\begin{aligned} \frac{dP_{CO_2}}{dt} &= R_1 = k_3P_{\cdot\text{CH}_3}\theta \\ &= \frac{k_1k_3P_{O_2}^{0.5}P_{\cdot\text{CH}_3}}{k_2P_{CH_4} + k_3P_{\cdot\text{CH}_3} + k_1P_{O_2}^{0.5}} \quad (13b) \end{aligned}$$

For every 27 cases, the rates of C<sub>2</sub> formation ( $R_2$ ) were rearranged as a function of

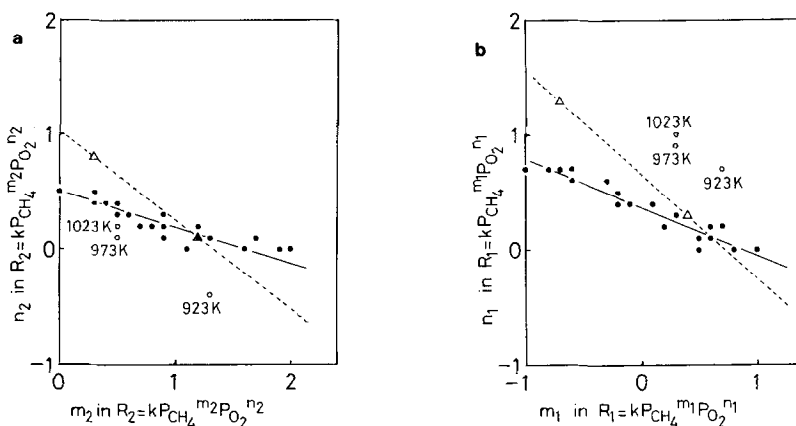


FIG. 5. (a) The relation between  $m_2$  and  $n_2$  ( $\text{CH}_4$  order and  $\text{O}_2$  order for  $\text{C}_2$  production rate, see text). The value was calculated by assuming that the rate of Eq. (1) was proportional to  $P_{\text{O}_2}^{0.5}$  (●) and to  $P_{\text{O}_2}$  (Δ). (○) Experimental values over 15% Na<sup>+</sup>-MgO. (b) The relation between  $m_1$  and  $n_1$  ( $\text{CH}_4$  order and  $\text{O}_2$  order for  $\text{C}_1$  production rate, see text). The value was calculated by assuming that the rate of Eq. (1) was proportional to  $P_{\text{O}_2}^{0.5}$  (●) and to  $P_{\text{O}_2}$  (Δ). (○) Experimental values over 15% Na<sup>+</sup>-MgO.

$P_{\text{CH}_4}$  and  $P_{\text{O}_2}$  using the power rate law expression. The 27 sets of the  $P_{\text{CH}_4}$  and  $P_{\text{O}_2}$  dependences (represented to as  $m_2$  and  $n_2$ ) were found to have some relationship,  $\frac{2}{3}m_2 + 2n_2 = 1$ , which is shown in Fig. 5a. For  $\text{C}_1$  oxide formation, the rates  $R_1$  were also rearranged into the power rate law expression. The 27 sets of  $P_{\text{CH}_4}$  and  $P_{\text{O}_2}$  dependences (represented to as  $m_1$  and  $n_1$ ) were also found to have a similar relation:  $m_1 + \frac{2}{3}n_1 = 1$ , this is shown in Fig. 5b.

As the second case, Eq. (1) was assumed to be first-order with respect to  $P_{\text{O}_2}$ . For this case, calculations similar to those above gave the relationships  $\frac{2}{3}m_2 + n_2 = 1$  and  $\frac{1}{2}(m_1 + 1) + \frac{2}{3}n_1 = 1$  (Figs. 5a and 5b).

The experimental data in Table 2 are also plotted in Figs. 5a and 5b. Clearly, these data do not obey either of the above two relationships. Therefore, it does not seem that this reaction can be explained by the multiple-redox mechanism model.

## DISCUSSION

### Rideal-Redox Mechanism

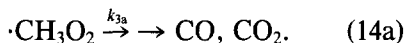
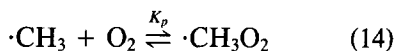
It was shown that the kinetic data over Na<sup>+</sup>-doped MgO catalyst can be expressed by the rate equation based on the Rideal-

redox mechanism. Sinev *et al.* have reported that the rate of  $\text{CH}_4$  conversion (but not the rates of  $\text{C}_2$  and  $\text{C}_1$  formation) over  $\text{PbO-Al}_2\text{O}_3$  is expressed by rate equations involving a  $\text{CH}_4\text{-O}_2$  redox cycle (2, 3). They reported activation energies for MO ( $M = \text{metal}$ ) reduction (Eq. (2)) of  $31.5 \pm 2.5$  kcal/mol and for M oxidation (Eq. (1)) of  $73.5 \pm 3.5$  kcal/mol. That means that the oxidation of catalyst proceeds preferably at higher temperature. In this study, we obtained an activation energy for MO reduction (on 15% Na<sup>+</sup>-MgO) of  $36 \pm 3$  kcal/mol and for M oxidation of  $18 \pm 3$  kcal/mol. This means that the catalyst is more reduced or has more bare sites at higher temperatures, which seems reasonable. The simulated value of  $k_2$  is lower than that of  $k_1$  at 923 K, while that of  $k_2$  is higher than that of  $k_1$  at 1023 K.

What is the meaning of redox of the MgO catalyst (15% Na<sup>+</sup>-MgO) used here? Since MgO itself is a stable oxide even at 1023 K, the reduction of MgO means the formation of coordinatively unsaturated  $\text{Mg}^{2+}$  ions on the surface. These surface  $\text{Mg}^{2+}$  ions would be covered by oxygen in the "oxidized state." Another explanation might be that Na<sup>+</sup> ions act as an oxygen reservoir

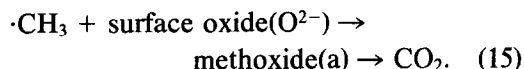
(for example  $\text{Na}_2\text{O} + 0.5 \text{O}_2 = 2 \text{Na}^+\text{O}^-$ ,  $\text{Na}_2\text{O} + 1.5 \text{O}_2 = 2 \text{NaO}_2$ , or  $\text{Na}_2\text{O} + 0.5 \text{O}_2 = \text{Na}_2\text{O}_2$ ). However, we prefer the first model, in which MgO itself is the active center rather than the alkali ion as has been discussed in the previous paper (11).

What about the value of  $k_4/k_3^2$ , which is assumed to decide the selectivity of  $\text{C}_2$  hydrocarbons against  $\text{C}_1$  oxides? The results in Table 3 show that  $k_4/k_3^2$  has a temperature coefficient of 14 kcal/mol. If Eq. (4) is a simple gas phase reaction of  $\cdot\text{CH}_3$  combination, which has been reported to have a very low activation energy ( $\approx 0$ ), the apparent activation energy of  $k_3$  is  $-7$  kcal/mol. This apparent negative activation energy of  $k_3$  may be explained as follows. If  $\text{O}_2$  is present,  $\cdot\text{CH}_3$  is easily converted to  $\cdot\text{CH}_3\text{O}_2$ : this process is believed to be almost in equilibrium (Eq. (14)) (37, 38). We assume that  $\text{CO}_2$  is mostly produced by decomposition of  $\cdot\text{CH}_3\text{O}_2$ . Now Eq. (3) ( $k_3$ ) is assumed to be composed of



Thus,  $k_3$  is represented as  $k_{3a}K_p$ . Since  $\Delta H$  for  $K_p$  has been reported to be  $-32$  kcal/mol (37, 38), the apparent activation energy of  $k_{3a}$  is thus assumed to be 25 kcal/mol. At a high temperature, the equilibrium condition moves the system far to the left in Eq. (14). The ratio  $\cdot\text{CH}_3\text{O}_2/\cdot\text{CH}_3$  is considered to be about 2% under the reaction conditions at 1023 K. Lunsford and colleagues have speculated that the similar mechanisms occur over  $\text{Li}^+\text{-MgO}$  and  $\text{Na}^+\text{-CaO}$  catalysts (6, 39).

If Eqs. (14) and (14a) only govern  $\text{CO}_2$  formation, the value of  $x$  in Eq. (3) must be 2. Since the experimental value obtained is not 2 but 1.6, another path must also occur, for example the reaction of  $\cdot\text{CH}_3$  with the surface:



Although there are some ambiguous points, such that  $x$  is not 2, which suggest some contribution of Eq. (15), the Rideal-redox mechanism seems to be the most adequate mechanism and useful for the discussion of the  $\text{C}_2/\text{C}_1$  selectivity.

Sinev *et al.* recently proposed a very similar treatment(40). In their work, the rate of  $\text{C}_1$  formation is proportional to the square of methyl peroxide concentration, while it is first-order in our treatment.

#### Langmuir-Hinshelwood Mechanism

The kinetic data obtained over 15%  $\text{Na}^+\text{-MgO}$  could also be explained by using the Langmuir-Hinshelwood mechanism. Here we have to check the meaning of the rate constants. As shown in Table 4,  $k_2K_0K_m$  does not seem to depend much on the reaction temperature. The value of  $k_2$  is clearly higher at higher temperatures, because it is the rate constant of Eq. (2a). However,  $K_0$  and  $K_m$  are clearly lower at high temperatures, because they are the adsorption equilibrium constants. As a result,  $k_2K_0K_m$  is relatively constant in the temperature range 923 to 1023 K. We cannot derive individual values for  $k_2$ ,  $K_0$ , and  $K_m$  by this method. Thus, this approach gives less information than the Rideal-redox mechanism.

From the nature of the adsorption equilibrium in Eqs. (5a) and (6a), the values of  $p$  and  $q$  must be higher (weak adsorption) at higher temperatures. However, although the value of  $p$  is higher at the higher temperatures, the value of  $q$  is not. Note that the value of  $p$  is greater than 0.5, indicating that oxygen should be adsorbed as the molecular species,  $\text{O}_2(\text{a})$ , instead of as the atomic species,  $\text{O}(\text{a})$ . This result is very similar to the results for the rate of  $\text{CH}_4$  oxidation over several catalysts, for example,  $\text{Sm}_2\text{O}_3$  (1), where the active oxygen species was reported to be  $\text{O}_2(\text{a})$ . At present, it is hard to decide the form of active oxygen. This model also can give the information about  $\text{C}_2/\text{C}_1$  selectivity in a simple form. Overall, the Langmuir-Hinshelwood mechanism

leaves several ambiguous points, although it can be applied numerically.

### Pressure Dependence

Our kinetic data were well expressed by the rate equation based on the Rideal-redox mechanism. The rate equations (Eqs. (12) and (13)) may be rewritten using a constant  $x = 1.6$  as

$$\frac{dP_{C_2H_6}}{dt} = R_2 = \frac{k_3^2 P_{O_2}^{1.6}}{16k_4} \left( \left( 1 + \frac{8k_1 k_2 k_4 P_{O_2} P_{CH_4}}{k_3^2 P_{O_2}^{1.6} (k_1 P_{O_2} + k_2 P_{CH_4})} \right)^{0.5} - 1 \right)^2 \quad (12c)$$

$$\frac{dP_{CO_2}}{dt} = R_1 = \frac{k_3^2 P_{O_2}^{1.6}}{4k_4} \left( \left( 1 + \frac{8k_1 k_2 k_4 P_{O_2} P_{CH_4}}{k_3^2 P_{O_2}^{1.6} (k_1 P_{O_2} + k_2 P_{CH_4})} \right)^{0.5} - 1 \right). \quad (13c)$$

The sum of  $R_1 + 2R_2$  gives  $-dCH_4/dt$ , which leads the rate of  $CH_4$  conversion, as

$$-\frac{dP_{CH_4}}{dt} = \frac{k_1 P_{O_2} k_2 P_{CH_4}}{k_1 P_{O_2} + k_2 P_{CH_4}}. \quad (16)$$

We then tried to transform the Eqs. (12c), (13c), and (16) to the power rate form using an approximation method, in order to compare the experimental data of power rate form. Table 5 shows the results. The orders in Table 5 are given as ranges because they were calculated by an approximation. Note that the  $CH_4$  power in  $C_2$  formation is higher than the  $CH_4$  power in  $C_1$  formation, because 1 mol of  $C_2$  is formed by 2 mol of  $\cdot CH_3$ . It is also interesting to note that the  $O_2$  order in  $C_2$  formation can be negative. Indeed, the data at 923 K give a negative order ( $-0.4$  in Table 2). A negative order is also seen on  $SrCO_3$  (41). Similar results were reported by Ito *et al.* (6) and Hinsien *et al.* (13). Our experimental values (Table 2) are all within the range of the calculated values (Table 5). Therefore, the results of the power rate form are well explained by the Rideal-redox mechanism.

TABLE 5

Reaction Orders for  $R_{CH_4}$ ,  $R_2$ , and  $R_1$  Calculated on the Basis of the Rideal-Redox Mechanism on 0.0165 or 0.05 g of 15% Na<sup>+</sup>-MgO at 923 to 1023 K

	Order	
	$CH_4$	$O_2$
$R_{CH_4}^a$	0-1	0-1
$R_2^b$	0-2	-1.6-1
$R_1^c$	0-1	0-1.3

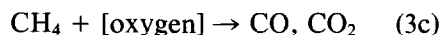
<sup>a</sup>  $2R_2 + R_1$  (rate of methane consumption).

<sup>b</sup> Rate of  $C_2$  hydrocarbon formation.

<sup>c</sup> Rate of  $C_1$  oxide formation.

### Possible Independent Path to $CO_2$

So far we have analyzed three reaction models that assume a common intermediate to both  $C_2$  and  $C_1$  compounds. This assumption was based on the fact that  $C_2$  hydrocarbons and  $CO_2$  start to form at the same temperature over the Na<sup>+</sup>-MgO catalyst (7). Now we discuss the possibility of an independent path to  $CO_2$  (step 0 in the initial scheme) from a kinetic viewpoint. As a matter of convenience, we assume that  $C_2$  hydrocarbons are formed as in the Rideal-redox mechanism (Eqs. (1), (2), and (4)). However, Eq. (3) is replaced by the reaction



Thus, assuming that the concentration of surface [oxygen] is identical to  $\theta$  in Eq. (6) and using the steady-state treatment for  $\cdot CH_3$  in Eqs. (2) and (4), the following equations are obtained:

$$\frac{dP_{\cdot CH_3}}{dt} = \frac{k_1 P_{O_2} k_2 P_{CH_4}}{k_1 P_{O_2} + k_2 P_{CH_4}} - 2k_4 P_{\cdot CH_3}^2 = 0 \quad (7c)$$

$$\frac{dP_{C_2H_6}}{dt} = R_2 = k_4 P_{\cdot CH_3}^2 = \frac{k_1 k_2 P_{O_2} P_{CH_4}}{2(k_1 P_{O_2} + k_2 P_{CH_4})}. \quad (12d)$$

The rate of  $CO_2$  formation (Eq. (3c)) is inde-

pendent of  $C_2$  formation. It should be described as

$$\frac{dP_{CO_2}}{dt} = R_1 = k_3 P_{O_2}^y P_{CH_4}^z \quad (13d)$$

This model suggests that any orders with respect to  $P_{CH_4}$  and  $P_{O_2}$  should be positive for  $C_2$  or the  $CO_2$  production rate. However, as shown in Table 2, the experimental results sometimes give negative orders with respect to  $P_{O_2}$  for  $C_2$  hydrocarbon formation. Therefore, this reaction model is not applicable to the reaction over  $Na^+-MgO$  at higher temperatures. However, if the reaction is performed at low temperatures especially over transition-metal-doped  $MgO$ , the surface reaction to give  $CO_2$  by way of surface methoxide may be important (42).

It has been pointed out that the  $CH_4$  order for  $C_2$  hydrocarbon formation is higher than that for  $C_1$  oxides in any model with a common intermediate. The results in Table 2 show this tendency, which results from the fact that 2 mol of  $\cdot CH_3$  give 1 mol of  $C_2H_6$ , whereas 1 mol of  $\cdot CH_3$  gives 1 mol of  $C_1$  oxides. On the other hand, this constraint does not hold for the independent reaction model. Since all  $\cdot CH_3$  reacts to give  $C_2$  hydrocarbons in this model, the  $CH_4$  order for  $C_2$  formation is between 0 and unity (Eq. (12d)), and the  $CH_4$  order for  $C_1$  oxide formation ( $z$ ) is also between 0 and unity. Thus,  $CH_4$  orders seem to be much the same in the two rate equations. In this sense, this model does not agree with the experimental results (Table 2).

#### Effect of Specific Surface Area on Selectivity

It has been shown that among  $MgO$  catalysts doped with various elements, catalysts with low specific surface area have higher  $C_2$  selectivity at a similar conversion level (about 100%  $O_2$  conversion). It has been suggested that this fact is due to the heterogeneous-homogeneous reaction mechanism (7, 10, 11). In this section, the surface area effect will be discussed through the Rideal-redox mechanism. We

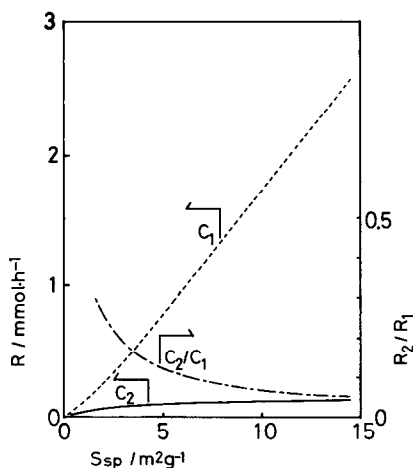


FIG. 6.  $R_2$  (rate of  $C_2$  hydrocarbon formation),  $R_1$  (rate of  $C_1$  oxide formation), and  $R_2/R_1$  as a function of  $S_{sp}$  (specific surface area) for a constant catalyst weight (0.05 g). One point is a real datum (1023 K,  $P_{CH_4} = 2.72$  kPa,  $P_{O_2} = 1.36$  kPa,  $S_{sp} = 2$  m<sup>2</sup> g<sup>-1</sup>,  $W = 0.05$  g).

consider the rate ratio of  $C_2$  hydrocarbons to  $C_1$  compounds,  $R_2/R_1$ , which is derived by Eqs. (9) to (13):

$$\frac{R_2}{R_1} = \frac{1}{4} \left( \left( 1 + \frac{8k_1k_2k_4P_{O_2}P_{CH_4}}{k_3^2P_{O_2}^x(k_1P_{O_2} + k_2P_{CH_4})} \right)^{0.5} - 1 \right) \quad (17)$$

If all processes (Eq. (1) to (4)) are surface reactions,  $R_2/R_1$  does not depend on the specific surface area,  $S_{sp}$ . If any process is not a surface reaction; however,  $R_2/R_1$  could be a function of  $S_{sp}$ . If the  $\cdot CH_3$  coupling process ( $k_4$ ) is a gas phase reaction and the  $CO_2$  formation process ( $k_3$ ) needs the surface (probably through Eq. (14a)), then  $k_1$ ,  $k_2$ , and  $k_3$  are proportional to  $S_{sp}$ , but  $k_4$  is independent of  $S_{sp}$ . In this case,  $R_2/R_1$  changes as a function of  $S_{sp}$  as predicted by Eq. (17). The value of  $R_2/R_1$  is higher at low  $S_{sp}$ . By Eqs. (12c) and (13c),  $R_2$  and  $R_1$  can also be expressed as functions of  $S_{sp}$ .

Suppose we could make various catalysts have the same chemical properties but different specific surface areas ( $S_{sp}$ ). Figure 6 demonstrates how the production rates ( $R_2$ ,

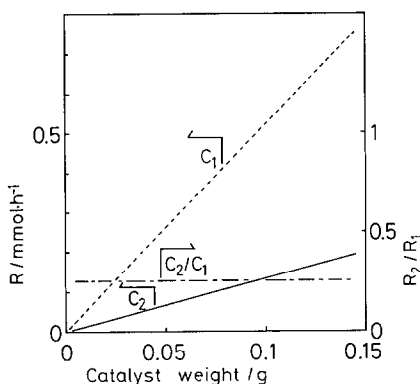


FIG. 7.  $R_2$  (rate of  $C_2$  hydrocarbon formation),  $R_1$  (rate of  $C_1$  oxide formation), and  $R_2/R_1$  as a function of catalyst weight for constant  $S_{sp}$  ( $2 \text{ m}^2 \text{ g}^{-1}$ ). One point is a real datum ( $1023 \text{ K}$ ,  $P_{\text{CH}_4} = 2.72 \text{ kPa}$ ,  $P_{\text{O}_2} = 1.36 \text{ kPa}$ ,  $S_{sp} = 2 \text{ m}^2 \text{ g}^{-1}$ ,  $W = 0.05 \text{ g}$ ).

$R_1$ ) and selectivity ( $R_2/R_1$ ) would change if we could change  $S_{sp}$  at a constant catalyst weight and volume. These results are based on the above assumptions and the kinetic data at one point ( $1023 \text{ K}$ ,  $P_{\text{CH}_4} = 2.72 \text{ kPa}$ ,  $P_{\text{O}_2} = 1.36 \text{ kPa}$ ,  $S_{sp} = 2 \text{ m}^2 \text{ g}^{-1}$ ,  $W = 0.05 \text{ g}$ ).  $R_1$  is almost proportional to  $S_{sp}$ , but  $R_2$  gradually approaches saturation.  $R_2/R_1$  is higher when  $S_{sp}$  is small. In this calculation, the value at  $S_{sp} = 2 \text{ m}^2 \text{ g}^{-1}$  is the only real value from the experiment.

Next, we suppose that the secondary re-

action ( $C_2$  to  $C_1$  oxides) and reactant pressure drop could be neglected even at high conversion (high  $W/F$ ). Thus,  $R_2$  and  $R_1$  are proportional to the catalyst weight (or contact time), and  $R_2/R_1$  is independent of the catalyst weight. Figure 7 shows this relation:  $R_2$ ,  $R_1$ , and  $R_2/R_1$  as a function of the catalyst weight ( $W$ ) where  $S_{sp}$  of the catalyst ( $2 \text{ m}^2 \text{ g}^{-1}$ ) and the total flow rate ( $F = 55 \text{ ml/min}$ ) are constant. The value of  $2 \text{ m}^2 \text{ g}^{-1}$  is the real value of  $S_{sp}$  for the 15% Na<sup>+</sup>-MgO catalyst used in this reaction.  $R_2$  and  $R_1$  reach values where  $\text{O}_2$  conversion would be 100% at some catalyst weight. By assuming the above method,  $R_2$ ,  $R_1$ , and the catalyst weight that gives 100%  $\text{O}_2$  conversion were calculated for various catalysts having various  $S_{sp}$ . The results are shown as a function of  $S_{sp}$  in Figs. 8a and 8b. When  $S_{sp}$  is high, a smaller weight of catalyst gives 100%  $\text{O}_2$  conversion. As shown in Fig. 8a, the catalyst with  $S_{sp} = 0.3 \text{ m}^2 \text{ g}^{-1}$  achieves 100%  $\text{O}_2$  conversion at a 2-g catalyst weight. To compare these calculations to the practical data,  $R_2/R_1$  was calculated for 2 g of catalyst with various  $S_{sp}$  (Fig. 8b). In Fig. 8b, for  $S_{sp}$  less than  $0.3 \text{ m}^2 \text{ g}^{-1}$ , the reactions are progressive; that is,  $R_2$  increases with increasing  $S_{sp}$  as long as  $\text{O}_2$  conversion is less than 100%. However,  $\text{O}_2$  conversion reaches 100% at  $S_{sp} = 0.3 \text{ m}^2$

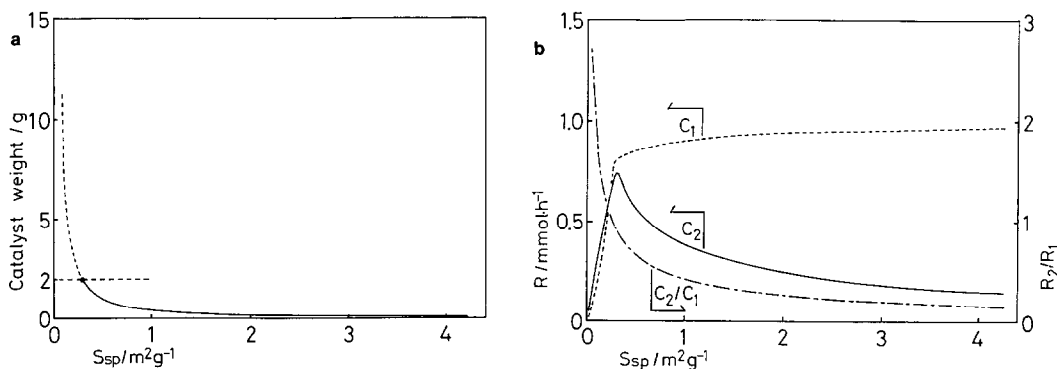


FIG. 8. (a) The catalyst weight necessary to get 100%  $\text{O}_2$  conversion as a function of  $S_{sp}$  ( $1023 \text{ K}$ ). Reactant pressure drop and secondary reactions are neglected (see text). (b)  $R_2$ ,  $R_1$ , and  $R_2/R_1$  over 2 g of catalyst with various  $S_{sp}$  ( $1023 \text{ K}$ ). The value for  $S_{sp} > 0.3 \text{ m}^2/\text{g}$  is calculated at 100%  $\text{O}_2$  conversion. Reactant pressure drop and secondary reaction are neglected (see text).

$\text{g}^{-1}$ , after which  $R_2$  decreases with increasing  $S_{\text{sp}}$  ( $S_{\text{sp}} > 0.3 \text{ m}^2 \text{ g}^{-1}$ ). In this way, the  $\text{C}_2$  hydrocarbon yield has a maximum at a suitable  $S_{\text{sp}}$  under these conditions (if reactant pressure drop can be neglected).

Indeed, this tendency is seen in the data obtained over various MgO catalysts (7, 10). A similar specific surface area effect has been reported for the  $\text{C}_2$  formation from  $\text{CH}_4$  pyrolysis (43). Strictly speaking, the specific surface area effect is much more pronounced for the calculated result (Fig. 8) than for the actual data (7, 10). One reason may be overestimation of the surface dependence with respect to  $\text{CO}_2$  formation from  $\cdot\text{CH}_3$  (Eq. 3) ( $k_3$  is proportional to  $S_{\text{sp}}$ ). Lunsford and colleagues suggest that the  $\text{C}_2$  hydrocarbon selectivity would be a function of  $1/(S + \text{constant})$  (personal communication, 1987).  $\text{CO}_2$  formation may occur by the oxidation of  $\cdot\text{CH}_3\text{O}_2$  in the gas phase. Although there are some other assumptions (reactant pressure drop and secondary reaction are neglected), the specific surface area effect would be qualitatively well explained by the Rideal-redox mechanism where  $\cdot\text{CH}_3$  coupling occurs in the gas phase. The  $\text{C}_2$  hydrocarbon yield decreases with increasing  $S_{\text{sp}}$  under the condition that  $\text{O}_2$  conversion is constant even if the conversion is less than 100%, because  $R_2/R_1$  decreases with increasing  $S_{\text{sp}}$ .

#### CONCLUSION

Oxidative coupling of  $\text{CH}_4$  over 15%  $\text{Na}^+ \text{-MgO}$  can be explained by using the Rideal-redox mechanism, which includes heterogeneous and homogeneous steps. The production of gaseous  $\cdot\text{CH}_3$ , the intermediate, would be a heterogeneous process (surface reaction), and the production of  $\text{C}_2$  hydrocarbons, the coupling of  $\cdot\text{CH}_3$ , would be a homogeneous process (gas phase reaction). The activity of the catalyst is related to the rate of oxidation of the surface ( $k_1$ ) and the rate of reaction between surface oxygen and  $\text{CH}_4$  ( $k_2$ ), and the selectivity is related to the rate ratio of methyl coupling and methyl oxidation ( $k_4/k_3^2$ ). These con-

stants are easily obtained from the flow experiments. The specific surface area (surface structure) seems to control both the reaction space, where coupling of  $\cdot\text{CH}_3$  (gas phase reaction  $k_4$ ) occurs preferably, and the surface, where oxidation of  $\cdot\text{CH}_3$  to  $\text{CO}_2$  (surface reaction  $k_3$ ) occurs preferably. This method of kinetic analysis can be applied to clarify the catalyst properties of various catalysts, which should be useful in reactor design.

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